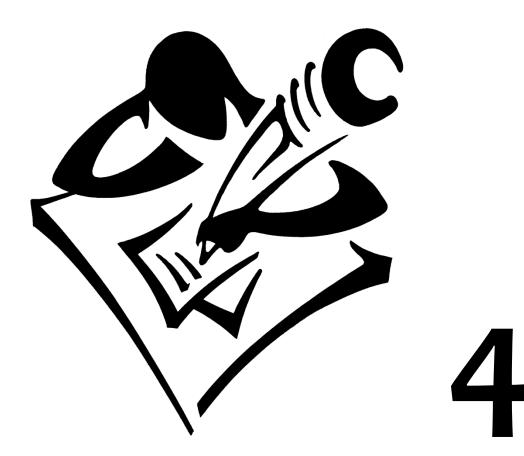
Tennessee Comprehensive Assessment Program

TCAP/CRA 2013



Anchor Set

Grade 4 – Raffle Tickets Task

SECURE MATERIAL - Reader Name:

Tennessee Comprehensive Assessment Program

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Part 2: Constructed Response Assessment

Raffle Tickets Task

Allexa sold 237 raffle tickets. Cayden sold 4 times as many raffle tickets as Allexa. How many raffle tickets did Cayden sell?

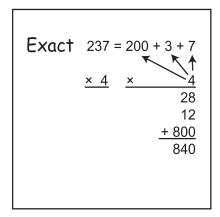
Estimated Number of Tickets by Rounding	Exact Number of Tickets





Part 2: Constructed Response Assessment

b. Shown below is a student's work for the exact solution to the problem:



Identify the mistake the student made in decomposing the number 237. Explain how this makes the student's exact solution incorrect.





Scoring Guide

The CCSS for Mathematical Content (3 points)

4.OA.A.2	Calculates accurately the exact number of tickets Cayden sold. (1 Point)	
4.NBT.A.1	Identifies the digit 3 as a misrepresentation of the value 30. (1 Point)	
4.NBT.A.3	Rounds 237 to 200 or 240 as part of the process of estimating the product of 237×4 .	
	OR	
	Rounds the calculated exact product accurately for the tens or hundreds place.	
	(1 Point)	

The CCSS for Mathematical Practice (2 points)

 MP3 Explains how the error in decomposition impacts the student's calculated solution.
(1 Point) (MP3: Construct viable arguments and critique the reasoning of others.)

MP4 Provides a diagram depicting four equal groups or a multiplication/repeated addition equation to explain the repetition of the number of tickets for the estimated or exact number of tickets. (1 Point)
(MP4: Model with mathematics.)

TOTAL POINTS: 5

The CCSS for Mathematical Content Addressed In This Task

Use the four operations with whole numbers to solve problems.		
4.OA.A.2	Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.	
Generalize place value understanding for multi-digit whole numbers.		
4.NBT.A.1	Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. For example, recognize that $700 \div 70 = 10$ by applying concepts of place value and division.	
4.NBT.A.3	Use place value understanding to round multi-digit whole numbers to any place.	

The CCSS for Mathematical Practice*

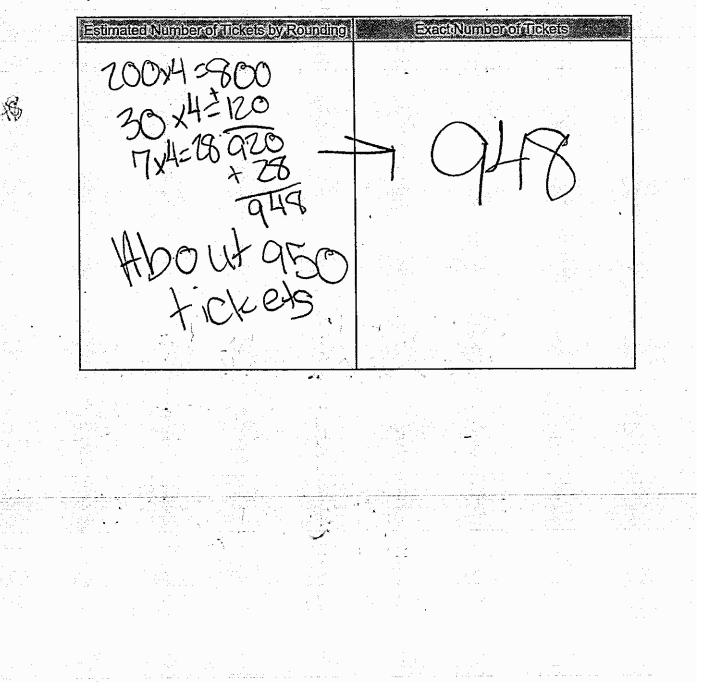
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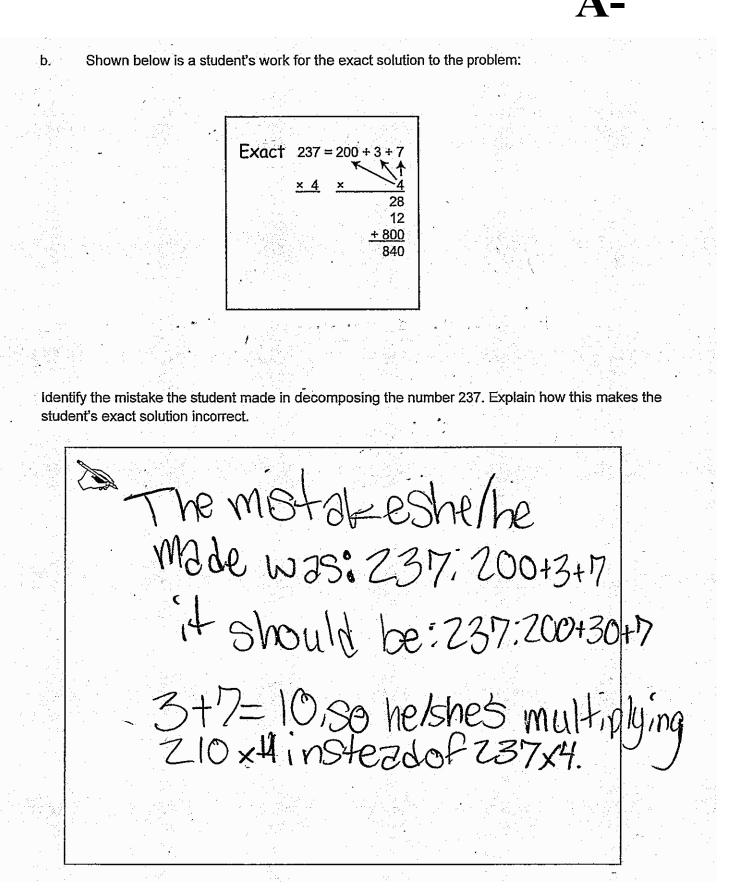
- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

* Gray type indicates Mathematical Practices not addressed in this assessment.

2. Raffle Tickets Task

Allexa sold 237 raffle tickets. Cayden sold 4 times as many raffle tickets as Allexa. How many raffle tickets did Cayden sell?





Anchor 1	Litho 0194
Total Content Points: 3	(4.OA.A.2, 4.NBT.A.1, 4.NBT.A.3)
Total Practice Points: 2	(MP3, MP4)

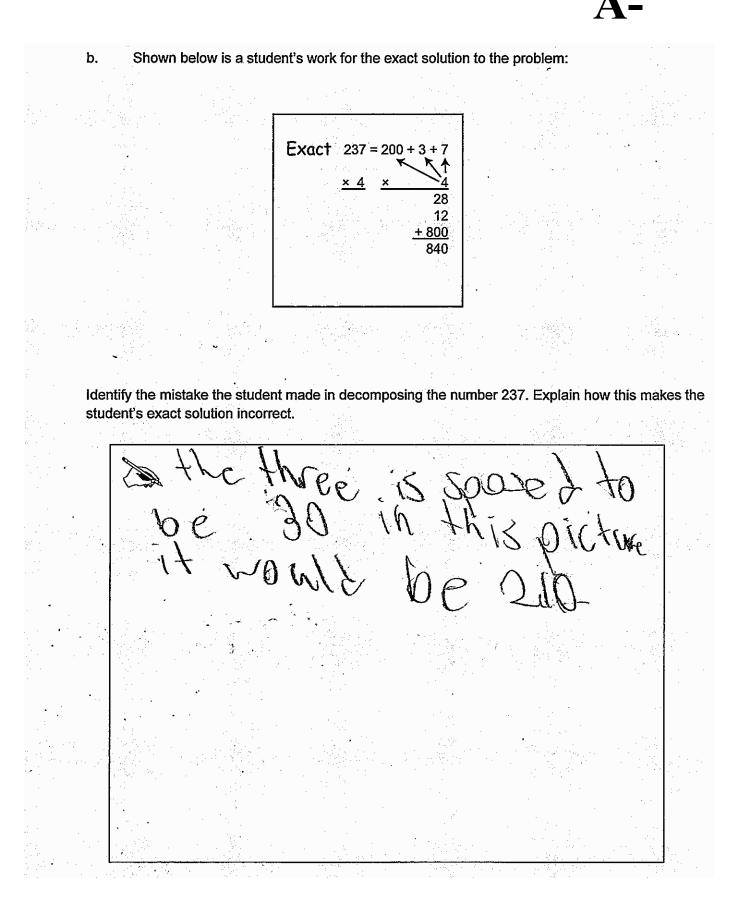
The student accurately calculates the exact number of tickets Cayden sold in Part A to solve a word problem involving multiplicative comparison $(237 \times 4 = 948)$ (4.OA.A.2). In Part B, the student identifies the digit 3 as a misrepresentation of the value 30, recognizing that in a multidigit whole number, a digit in one place represents ten times what it represents in the place to its right ("The mistake she/he made was: 237: 200 + 3 + 7 it should be: 237: 200 + 30 + 7") (4.NBT.A.1). The student uses place value understanding to accurately round the calculated exact product of 948 for the tens place to 950 in Part A (4.NBT.A.3). In Part B, the student adequately explains how the error in decomposition impacts the provided calculated solution by stating "3 + 7 = 10, so he/she's multiplying 210×4 instead of 237×4 ," suggesting an understanding that this uneven equation would lead to an incorrect solution (MP3). By providing a series of multiplication equations to represent 237×4 to find the exact number of tickets, the student adequately explains the repetition of the number of tickets.(MP4).

Total Awarded Points: 5 out of 5



Allexa sold 237 raffle tickets. Cayden sold 4 times as many raffle tickets as Allexa. How many raffle tickets did Cayden sell?

• • •



Anchor 2	Litho 0016
Total Content Points: 3	(4.OA.A.2, 4.NBT.A.1, 4.NBT.A.3)
Total Practice Points: 2	(MP3, MP4)

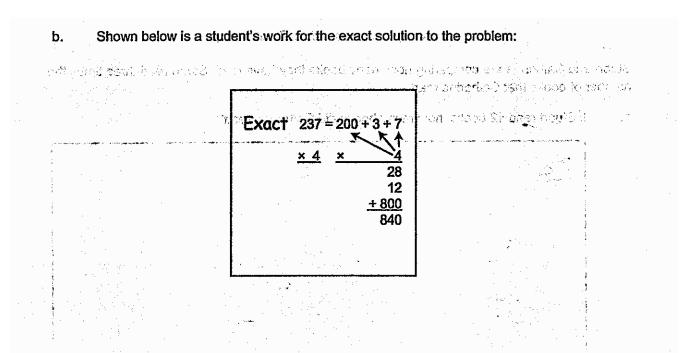
The student accurately calculates the exact number of tickets Cayden sold in Part A to solve a word problem involving multiplicative comparison $(237 \times 4 = 948)$ (4.OA.A.2). In Part B, the student identifies the digit 3 as a misrepresentation of the value 30, recognizing that in a multidigit whole number, a digit in one place represents ten times what it represents in the place to its right ("the three is sposed to be 30") (4.NBT.A.1). The student uses place value understanding to round 237 to 200 in Part A as part of the process of estimating the product of 237×4 ($200 \times 4 = 800$) (4.NBT.A.3). In Part B, the student adequately explains how the error in decomposition impacts the provided calculated solution by stating "in this picture it would be 210," suggesting an understanding that 200 + 3 + 7 = 210, which is not equal to the 237 on the other side of the equation, leading to an incorrect solution (MP3). To explain the repetition of the number of tickets, the student provides equations that multiply by 4 in Part A for both the estimated ($200 \times 4 = 800$) and exact number ($237 \times 4 = 948$) of tickets (MP4).

Total Awarded Points: 5 out of 5



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Identify the mistake the student made in decomposing the number 237. Explain how this makes the student's exact solution incorrect.

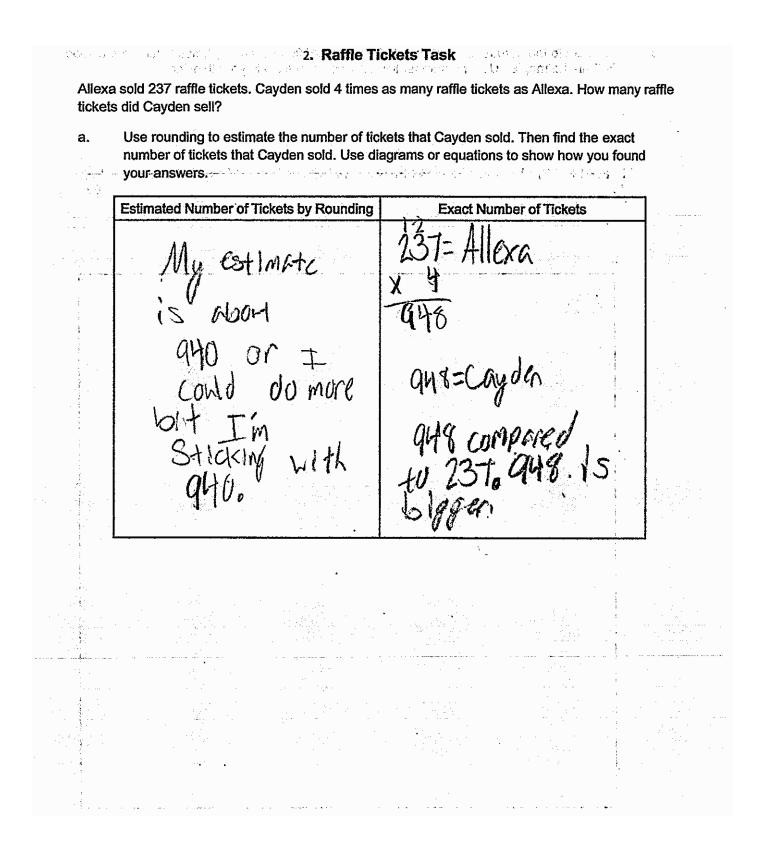
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Anchor 3	Litho 0085
Total Content Points: 2	(4.OA.A.2, 4.NBT.A.1)
Total Practice Points: 2	(MP3, MP4)

The student accurately calculates the exact number of tickets Cayden sold in Part A to solve a word problem involving multiplicative comparison $(237 \times 4 = 948)$ (4.OA.A.2). In Part B, the student identifies the digit 3 as a misrepresentation of the value 30, recognizing that in a multidigit whole number, a digit in one place represents ten times what it represents in the place to its right ("The mistake was that the student should have put a 30 where the 3 was") (4.NBT.A.1). The student uses incorrect place value understanding to improperly round 237 to 250 in Part A as part of the process of estimating the product of 237×4 ($250 \times 4 = 1000$) (no credit for 4.NBT.A.3). In Part B, the student adequately illustrates how the error in decomposition impacts the provided calculated solution through demonstrating the correct process (MP3). The student provides a multiplication equation in Part A that explains the repetition of the number of tickets for both the estimated ($250 \times 4 = 1000$) and exact ($237 \times 4 = 948$) number of tickets (MP4).

Total Awarded Points: 4 out of 5







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$\frac{x \cdot 4}{28} \times \frac{4}{28} \times \frac{137}{4}$	
$\frac{12}{+800}$ $\frac{+800}{840}$ $\frac{12}{847}$	
Identify the mistake the student made in decomposing the number 237. Explain how this make	es the
student's exact solution incorrect.	anta anta anta anta anta anta
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10+3,30°	
Helshe is incorrect.	

Anchor 4	Litho 0098
Total Content Points: 2	(4.OA.A.2, 4.NBT.A.1)
Total Practice Points: 1	(MP4)

The student accurately calculates the exact number of tickets Cayden sold in Part A to solve a word problem involving multiplicative comparison $(237 \times 4 = 948)$ (4.OA.A.2). In Part B, the student identifies the digit 3 as a misrepresentation of the value 30, recognizing that in a multidigit whole number, a digit in one place represents ten times what it represents in the place to its right ("it needs to be 200 + 30 + 7. not 3, 30") (4.NBT.A.1). The student uses incorrect place value understanding to improperly round the calculated exact product of 948 to 940 in Part A (no credit for 4.NBT.A.3). In Part B, the student does not adequately explain how the error in decomposition impacts the provided calculated solution; the explanation merely points out the erroneous value and lacks any specifics involving the calculations (no credit for MP3). The student provides a multiplication equation in Part A that explains the repetition of the number of tickets for the exact number of tickets ($237 \times 4 = 948$) (MP4).

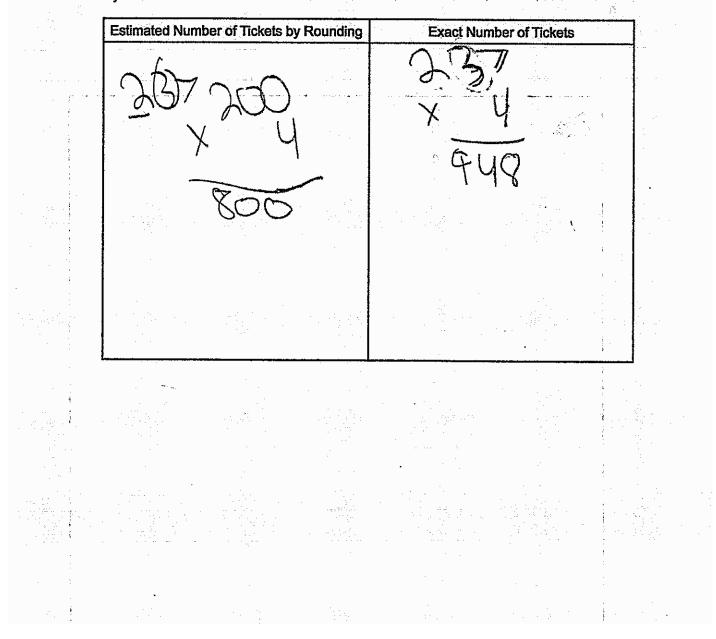
Total Awarded Points: 3 out of 5



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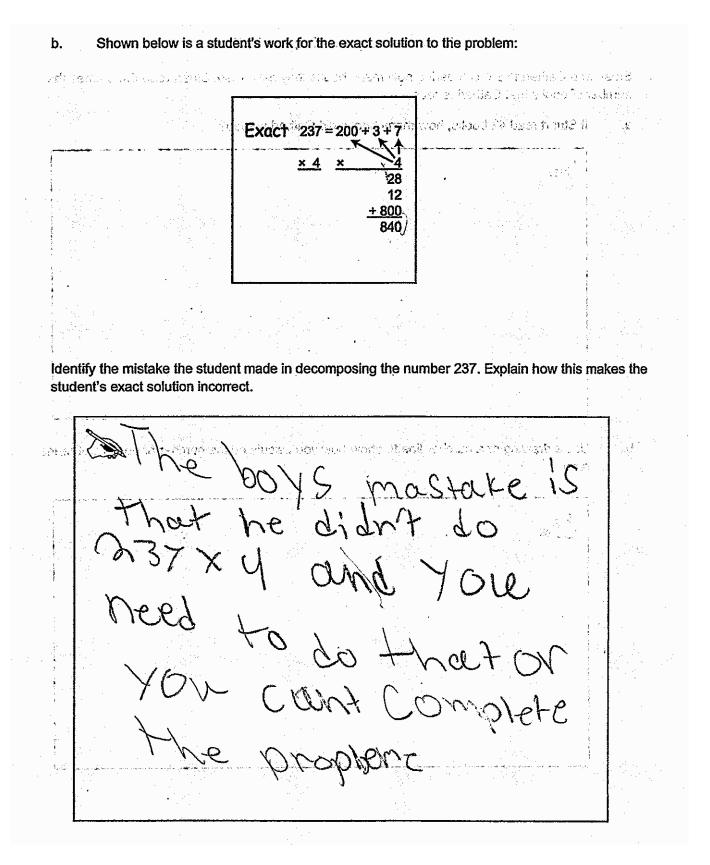
Allexa sold 237 raffle tickets. Cayden sold 4 times as many raffle tickets as Allexa. How many raffle tickets did Cayden sell?

a. Use rounding to estimate the number of tickets that Cayden sold. Then find the exact number of tickets that Cayden sold. Use diagrams or equations to show how you found your answers.



Litho#: 0096





Anchor 5	Litho 0096
Total Content Points: 2	(4.OA.A.2, 4.NBT.A.3)
Total Practice Points: 1	(MP4)

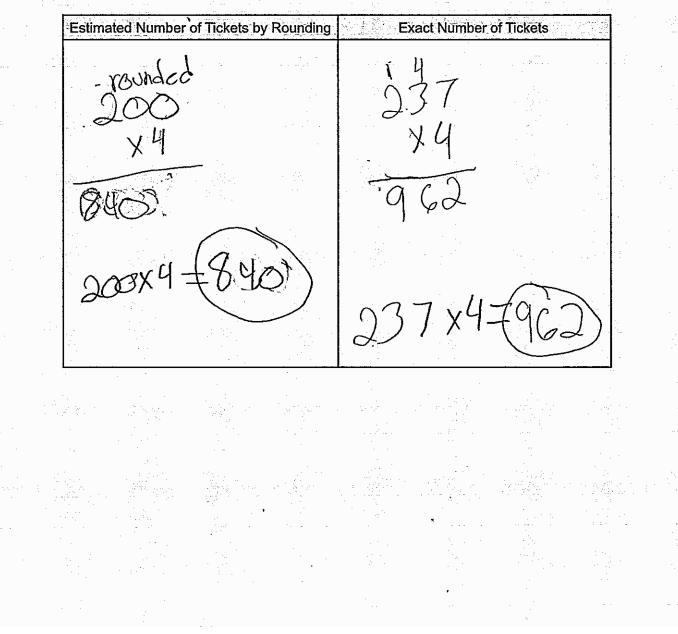
The student accurately calculates the exact number of tickets Cayden sold in Part A to solve a word problem involving multiplicative comparison $(237 \times 4 = 948)$ (4.OA.A.2). In Part B, the student does not identify the digit 3 as a misrepresentation of the value 30, showing no recognition that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right (no credit for 4.NBT.A.1). The student uses place value understanding to round 237 to 200 in Part A as part of the process of estimating the product of 237×4 ($200 \times 4 = 800$) (4.NBT.A.3). In Part C, the student does not adequately explain how the error in decomposition impacts the provided calculated solution (no credit for MP3). The student provides a multiplication equation in Part A that explains the repetition of the number of tickets for both the estimated ($200 \times 4 = 800$) and exact ($237 \times 4 = 948$) number of tickets (MP4).

Total Awarded Points: 3 out of 5

A- a

2. Raffle Tickets Task

Allexa sold 237 raffle tickets. Cayden sold 4 times as many raffle tickets as Allexa. How many raffle tickets did Cayden sell?





b. Shown below is a student's work for the exact solution to the problem:

Exact 237 = 200 + 3 + 7 $\times 4 \times 4$ 28 12 + 800840

Identify the mistake the student made in decomposing the number 237. Explain how this makes the student's exact solution incorrect.

7x4 does not = 28

Litho#: 0060

Anchor 6	Litho 0060
Total Content Points: 1	(4.NBT.A.3)
Total Practice Points: 1	(MP4)

The student incorrectly calculates the exact number of tickets Cayden sold in Part A to solve a word problem involving multiplicative comparison (no credit for 4.OA.A.2). In Part B, the student does not identify the digit 3 as a misrepresentation of the value 30, showing no recognition that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right (no credit for 4.NBT.A.1). The student uses place value understanding to round 237 to 200 in Part A as part of the process of estimating the product of $237 \times 4 (200 \times 4 = 840)$, and receives credit despite reaching an incorrect product (4.NBT.A.3). In Part C, the student does not correctly explain how the error in decomposition impacts the provided calculated solution (no credit for MP3). The student provides a multiplication equation in Part A that explains the repetition of the number of tickets for both the estimated $(200 \times 4 = 840)$ and exact $(237 \times 4 = 962)$ number of tickets, and receives credit despite neither equation having a correct product (MP4).

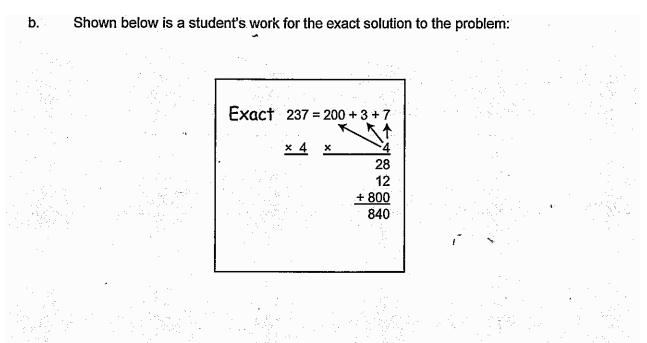
Total Awarded Points: 2 out of 5



Allexa sold 237 raffle tickets. Cayden sold 4 times as many raffle tickets as Allexa. How many raffle tickets did Cayden sell?

Exact Number of Tickets Estimated Number of Tickets by Rounding 190 2 I try 909





Identify the mistake the student made in decomposing the number 237. Explain how this makes the student's exact solution incorrect.

it Should 15 50 Post 42 that is >t mistake

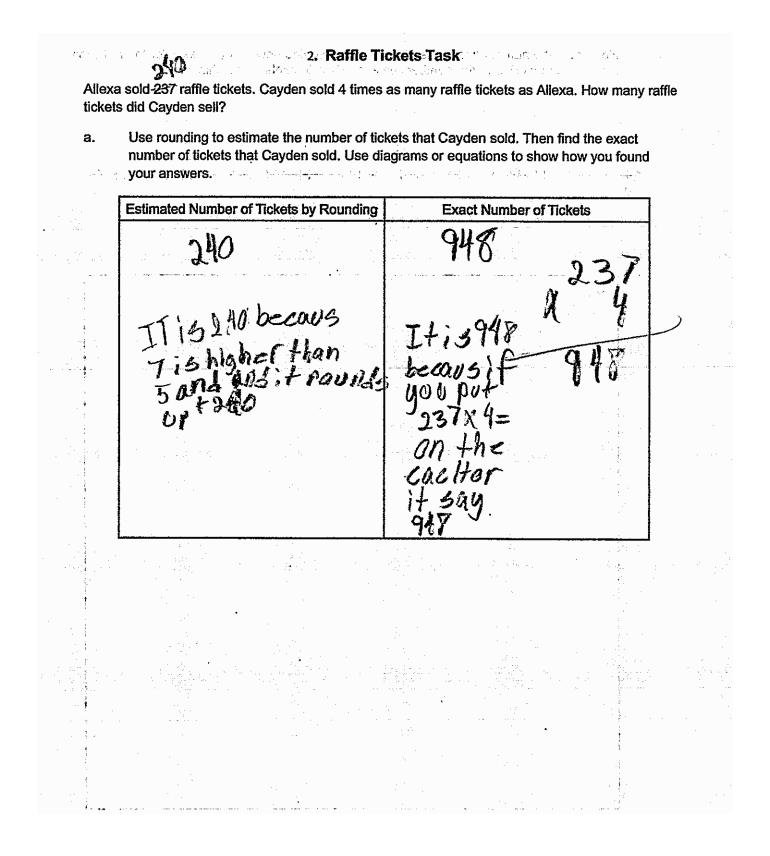
Litho#: 0031

Anchor 7	Litho 0031
Total Content Points: 1	(4.OA.A.2)
Total Practice Points: 1	(MP4)

The student accurately calculates the exact number of tickets Cayden sold in Part A to solve a word problem involving multiplicative comparison $(237 \times 4 = 948)$ (4.OA.A.2). In Part B, the student does not identify the digit 3 as a misrepresentation of the value 30, showing no recognition that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right (no credit for 4.NBT.A.1). The student does not use correct place value understanding to round 237 to any other value in Part A. While it could be inferred that the student was using 200 as part of the process of estimating the product of 237 × 4 given that a product of 800 was reached, it is necessary for the student to write the correct value in the equation (no credit for 4.NBT.A.3). In Part C, the student does not correctly explain how the error in decomposition impacts the provided calculated solution (no credit for MP3). The student provides a multiplication equation in Part A that explains the repetition of the number of tickets for the exact number of tickets ($4 \times 237 = 948$) (MP4).

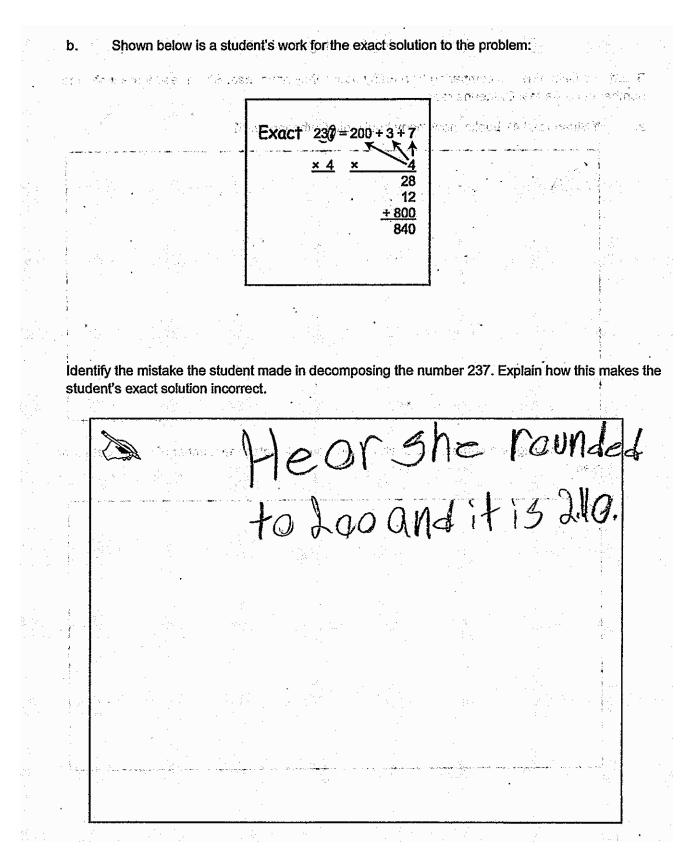
Total Awarded Points: 2 out of 5





Litho#: 0094





Anchor 8	Litho 0094
Total Content Points: 1	(4.OA.A.2)
Total Practice Points: 1	(MP4)

The student accurately calculates the exact number of tickets Cayden sold in Part A to solve a word problem involving multiplicative comparison $(237 \times 4 = 948)$ (4.OA.A.2). In Part B, the student does not identify the digit 3 as a misrepresentation of the value 30, showing no recognition that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right (no credit for 4.NBT.A.1). The student uses place value understanding to round 237 to 240 in Part A, but does not do it as part of the process of estimating the product of 237×4 (no credit for 4.NBT.A.3). In Part B, the student does not correctly explain how the error in decomposition impacts the provided calculated solution (no credit for MP3). The student provides a multiplication equation in Part A for the exact number of tickets ($237 \times 4 = 948$), which explains the repetition of the number of tickets (MP4).

Total Awarded Points: 2 out of 5

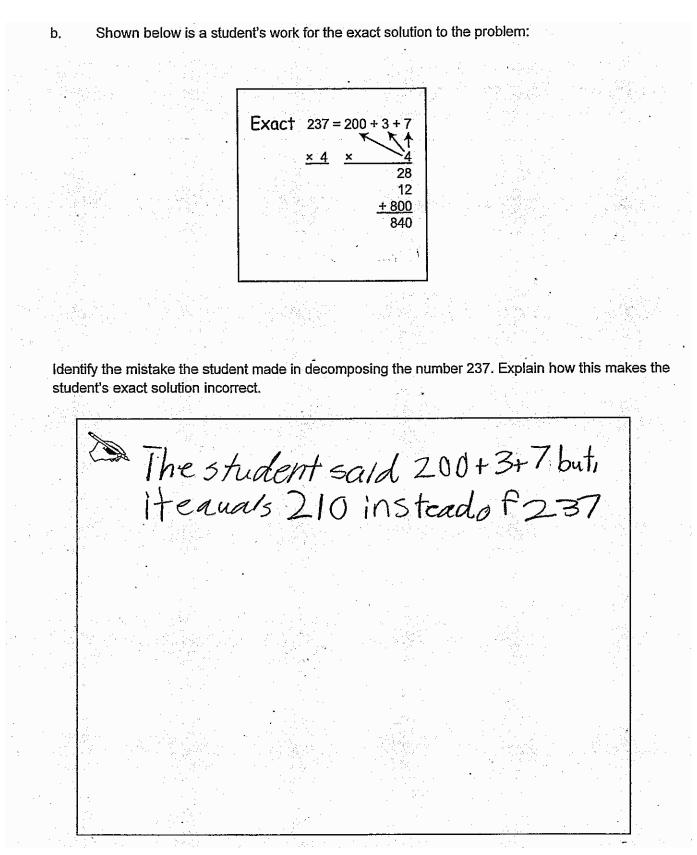


2. Raffle Tickets Task

Allexa sold 237 raffle tickets. Cayden sold 4 times as many raffle tickets as Allexa. How many raffle tickets did Cayden sell?

Estimated Number of Tickets by Rounding Exact Number of Tickets 237 rounded by 10-=240





Anchor 9	Litho 0214
Total Content Points: 0	
Total Practice Points: 1	(MP3)

The student does not accurately calculate the exact number of tickets Cayden sold in Part A to solve a word problem involving multiplicative comparison (no credit for 4.OA.A.2). In Part B, the student does not identify the digit 3 as a misrepresentation of the value 30, showing no recognition that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right (no credit for 4.NBT.A.1). The student uses place value understanding to round 237 to 240 in Part A, but does not do it as part of the process of estimating the product of 237×4 (no credit for 4.NBT.A.3). In Part B, the student adequately explains how the error in decomposition impacts the provided calculated solution by stating "the student said 200 + 3 + 7 but, it equals 210 instead of 237" (MP3). The student does not provide a diagram or a multiplication/repeated addition equation in Part A to explain the repetition of the number of tickets for either the estimated or exact number of tickets (no credit for MP4).

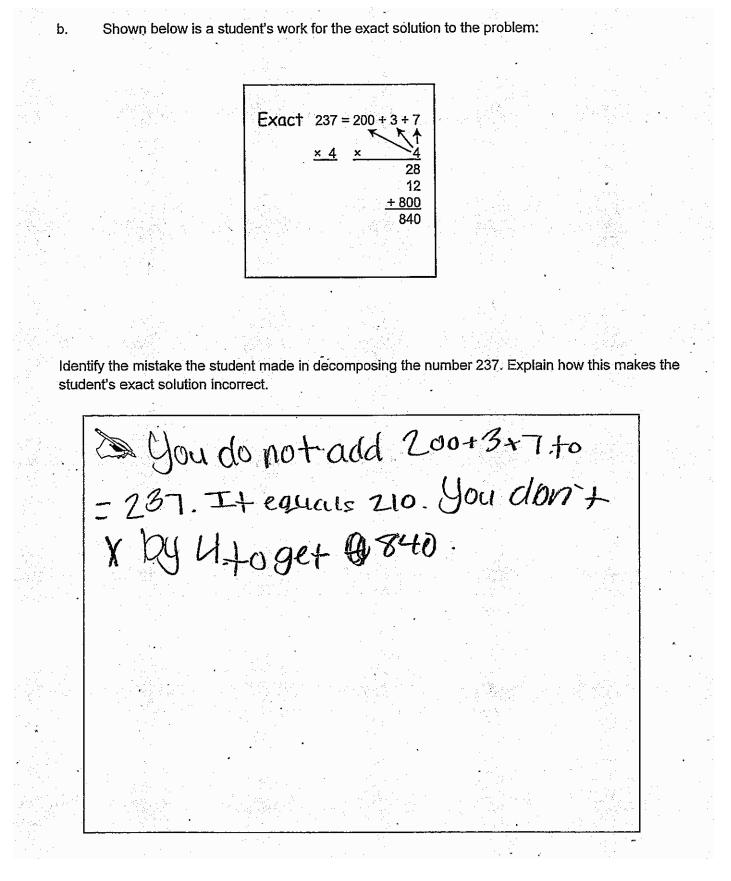
Total Awarded Points: 1 out of 5

A-1 a

2. Raffle Tickets Task

Allexa sold 237 raffle tickets. Cayden sold 4 times as many raffle tickets as Allexa. How many raffle tickets did Cayden sell?

Estimated Number of Hekels by Rounding: xactNumberofelickets



Anchor 10	Litho 0185
Total Content Points: 0	
Total Practice Points: 1	(MP3)

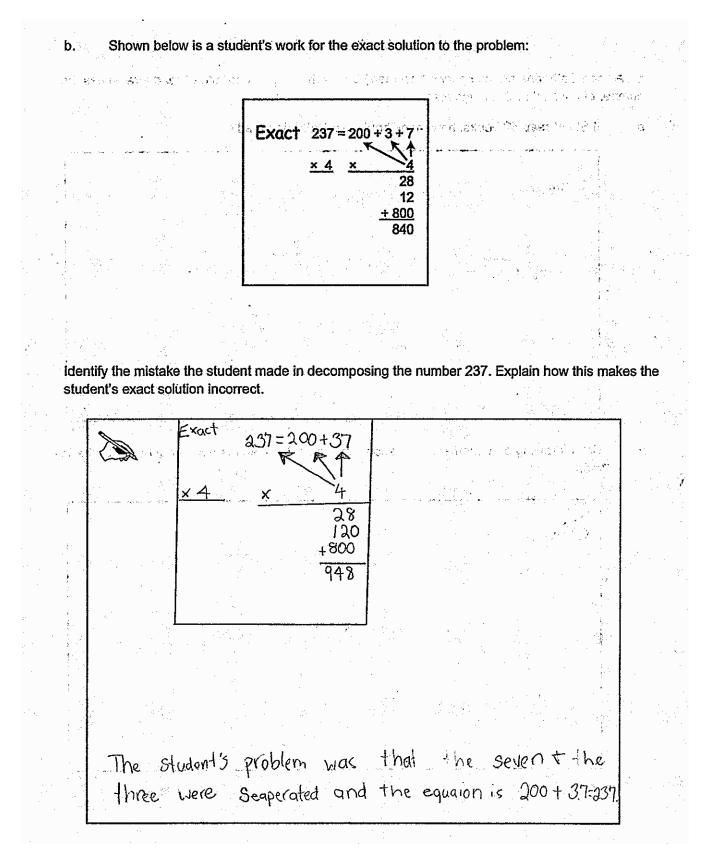
The student provides no calculations for the exact number of tickets Cayden sold in Part A, insufficiently demonstrating the ability to solve a word problem involving multiplicative comparison despite producing the correct answer (no credit for 4.OA.A.2). In Part B, the student does not identify the digit 3 as a misrepresentation of the value 30, showing no recognition that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right (no credit for 4.NBT.A.1). The student uses place value understanding to accurately round 948 to 950 in Part A, but the lack of any written calculations means that 948 cannot be considered a calculated exact product (no credit for 4.NBT.A.3). In Part B, the student adequately explains how the error in decomposition impacts the provided calculated solution by stating "You do not add 200 + 3 + 7 to = 237. It equals 210" (MP3). The student does not provide a diagram or a multiplication/repeated addition equation in Part A to explain the repetition of the number of tickets for either the estimated or exact number of tickets (no credit for MP4).

Total Awarded Points: 1 out of 5

A-1 a

a.	Use rounding to estimate the number of tic number of tickets that Cayden sold. Use dia your answers.			
-	Estimated Number of Tickets by Rounding	Exact Nur	nber of Tickets	
			100	
	I rounded up to two hundred, and fairly.	The exc is two Seven	act number undred, thirty-	
	I rounded up to two hundred, and fairly.	is two h		

A-1



Anchor 11 Litho 0080

Total Content Points: 0

Total Practice Points: 0

The student does not accurately calculate the exact number of tickets Cayden sold in Part A to solve a word problem involving multiplicative comparison (no credit for 4.OA.A.2). In Part B, the student does not identify the digit 3 as a misrepresentation of the value 30, showing no recognition that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right (no credit for 4.NBT.A.1). The student uses place value understanding to round 237 to 240 in Part A, but does not do it as part of the process of estimating the product of 237×4 , and the lack of calculations means it cannot be considered as a rounding of a calculated exact product (no credit for 4.NBT.A.3). In Part B, the student does not correctly explain how the error in decomposition impacts the provided calculated solution. The student's contention that the error is because "the seven & the three were seaperated" is not accurate. The separation of 3 and 7 is part of the process of finding the solution; the error is that they were separated incorrectly (no credit for MP3). The student does not provide a diagram or a multiplication/repeated addition equation in Part A to explain the repetition of the number of tickets for either the estimated or exact number of tickets (no credit for MP4).

Total Awarded Points: 0 out of 5