SECURE MATERIAL - Reader Name: $\qquad$ Tennessee Comprehensive Assessment Program

## TCAP/CRA

## 2014



## Phase II

Sharing Pizza Task Anchor Set

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## Sharing Pizza Task

Jenny, Kim, and Peter share two pizzas that are the same size. Jenny eats $\frac{5}{6}$ of a whole pizza, Kim eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.
a. Who eats more pizza, Peter or Jenny? Use <, >, or = to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use diagrams and words to explain how the numerator and denominator of the fractions can help you figure out which student eats more pizza.


## Sharing Pizza Task

Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kim claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter.

c. Explain with words and a diagram why you agree or disagree with Kim.


## Scoring Guide

## The CCSS for Mathematical Content (2 points)

3.NF.A.3d Compare two fractions with the same denominator by recording the results of the comparisons with the symbols > or <. Student may do this by:

- writing $\frac{5}{6}>\frac{4}{6}$ or $\frac{4}{6}<\frac{5}{6}$;
- showing the comparison of Kim's amount, $\frac{3}{6}$, to either $\frac{4}{6}$ or $\frac{5}{6}$ (although the student was not asked to compare Kim's amount, the student is still showing the ability to compare fractions).
(1 Point)
3.NF.A.3c States $\frac{2}{1}$ is 2 whole pizzas.
(1 Point)


## The CCSS for Mathematical Practice (3 points)

MP4 Creates an accurate diagram showing $\frac{5}{6}, \frac{4}{6}, \frac{2}{1}$, and $\frac{1}{2}$ (or $\frac{3}{6}$ if applicable).
(1 Point)
(MP4: Model with mathematics.)
MP6 Indicates a precise explanation of why one amount is greater than the other amount. The explanation makes reference to the denominators and the numerators of the fractions being compared.
(1 Point)
(MP6: Attend to precision).
MP7 Indicates in written explanation or diagram that $\frac{1}{2}$ is less than a whole and $\frac{2}{1}$ is two wholes.
(1 Point)
(MP7: Look for and make use of structure.)

TOTAL POINTS: 5

## The CCSS for Mathematical Content Addressed In This Task

## Develop understanding of fractions as numbers.

3.NF.A.3c Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. Examples: Express 3 in the form $3=3 / 1$; recognize that $6 / 1=6$; locate $4 / 4$ and 1 at the same point of a number line diagram.
3.NF.A.3d Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction model.

## The CCSS for Mathematical Practice*

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

* Gray type indicates Mathematical Practices not addressed in this assessment.

Sharing Pizza Task
Jenny, Kim, and Peter share two pizzas that are the same size. Jenny eats $\frac{5}{6}$ of a whole pizza, Kim eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.
a. Who eats more pizza, Peter or Jenny? Use $<_{1}>$, or $=$ to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use/diagrams andwyords to explain how the numerator and denominator of the fractions can help youffigure out which student eats more pizza.


Litho\#: 00263200144

Sharing Pizza Task
Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kim claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter.

c. Explain with/words and a diagram why you agree or disagree with Kim.


Litho\#: 00263200144

In Part A, the student correctly compares two fractions with the same denominator by recording the results of the comparison with the appropriate inequality symbol, writing " $\frac{4}{6}<\frac{5}{6}$ " (3.NF.A.3d). In Part B, the student states that $\frac{2}{1}$ is 2 whole pizzas (" $\frac{2}{1}=2$ pizzas") (3.NF.A.3c). The student creates accurate diagrams showing Jenny's $\frac{5}{6}$, Peter's $\frac{4}{6}$, and Kim's $\frac{3}{6}$ in Part B by labeling the individual slices with initials, showing $\frac{2}{1}$ in Part B, and showing $\frac{1}{2}$ in Part C (MP4). In Part A, the student indicates a precise explanation of why one amount is greater than the other amount by making reference to the denominators and the numerators of the fractions being compared ("Both of the fractions have the same denominator, so you look at the numerator to see which one is bigger. Jenny has a bigger numerator, so she ate more.") (MP6). In Part C, the student indicates that $\frac{1}{2}$ is less than a whole by creating a diagram showing a whole with only half shaded, and that $\frac{2}{1}$ is two wholes by showing 2 pizzas with a " 2 " pointing to them (MP7).

Total Awarded Points: 5 out of 5

## Sharing Pizza Task

Jenny, Kim, and Peter share two pizzas that are the same size. Jenny eats $\frac{5}{6}$ of a whole pizza, Kim eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.
a. Who eats more pizza, Peter or Jenny? Use $<,>$, or $=$ to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use diagrams and words to explain how the numerator and denominator of the fractions can help you figure out which student eats more pizza.


Sharing Pizza Task
Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kim claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter.

c. Explain with words and a diagram why you agree or disagree with Kim.


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Anchor 2
Litho 00063200145

Total Content Points: 2
(3.NF.A.3d, 3.NF.A.3c)

Total Practice Points: 2 (MP4, MP7)
In Part A, the student compares two fractions with the same denominator by drawing diagrams representing $\frac{5}{6}$ and $\frac{4}{6}$ and labeled accordingly, and then correctly using an inequality symbol to represent the relationship between them (3.NF.A.3d). In Part B, the student indicates that $\frac{2}{1}$ is 2 whole pizzas by stating, "you can get two 6 s out of 12 " and illustrating the point by drawing two number lines with $\frac{6}{6}$ circled on each of them (3.NF.A.3c). The student creates accurate diagrams showing $\frac{5}{6}$ and $\frac{4}{6}$ in Part A, and uses number lines in Part B showing $\frac{2}{1}$, and also in Part C to show $\frac{1}{2}$ (MP4). In Part A, by providing only a diagram without explaining further with words the relevance of the numerator and same denominator, the student does not indicate a precise explanation of why one amount is greater than the other amount, with reference to the denominators and the numerators of the fractions being compared (no credit for MP6). In Part B, the student indicates with two number lines that $\frac{2}{1}$ is two wholes, and in Part C, demonstrates with a number line that $\frac{1}{2}$ is less than a whole by showing $\frac{12}{12}$, circling $\frac{6}{12}$, and also labeling that as $\frac{1}{2}$ (MP7).

Total Awarded Points: 4 out of 5

## A-3a

## Sharing Pizza Task

Jenny, Kim, and Peter share two pizzas that are the same size. Jenny eats $\frac{5}{6}$ of a whole pizza, Kim eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.
a. Who eats more pizza, Peter or Jenny? Use $<,>$, or $=$ to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use diagrams and words to explain how the numerator and denominator of the fractions can help you figure out which student eats more pizza.


Sharing Pizza Task
Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kim claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter.

c. Explain with words and a diagram why you agree or disagree with Kim.


Total Content Points: 2 (3.NF.A.3d, 3.NF.A.3c)
Total Practice Points: 2 (MP4, MP7)
In Part A, the student compares two fractions with the same denominator by recording the results of the comparison with the appropriate inequality symbol, writing " $\frac{5}{6}>\frac{4}{6}$ " (3.NF.A.3d). In Part B, the student demonstrates that $\frac{2}{1}$ is 2 whole pizzas by writing " $\frac{2}{1}$ " with an arrow pointing to an illustration of 2 wholes (3.NF.A.3c). The student creates accurate number lines showing $\frac{5}{6}$ and $\frac{4}{6}$ in Part A, and diagrams showing $\frac{2}{1}$ in Part B and $\frac{1}{2}$ in Part C (MP4). While the student makes reference to denominators and numerators, one of the fractions is not problem-related ( $\frac{3}{5}$ ), and the explanation is unclear, thus not providing a precise explanation of why one amount is greater than the other amount (no credit for MP6). In Part B, the student indicates that $\frac{2}{1}$ is two wholes with a diagram. In Part C, the student indicates that $\frac{1}{2}$ is less than a whole by creating a diagram showing a whole with only half shaded (MP7).

Total Awarded Points: 4 out of 5

## A-4a

## Sharing Pizza Task

Jenny, Kim, and Peter share two pizzas that are the same size. Jenny eats $\frac{5}{6}$ of a whole pizza, Kim eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.
a. Who eats more pizza, Peter or Jenny? Use $<>$, or = to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use diagrams and words to explain how the numerator and denominator of the fractions can help you figure out which student eats more pizza.


Sharing Pizza Task
Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kim claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter.

c. Explain with words and a diagram why you agree or disagree with Kim.


Total Content Points: 2 (3.NF.A.3d, 3.NF.A.3c)
Total Practice Points: 2 (MP4, MP7)
In Part A, the student compares two fractions with the same denominator by recording the results of several comparisons and showing that Jenny's share was more than Peter's share with the appropriate inequality symbol, writing " $\frac{4}{6}<\frac{5}{6}$ " (3.NF.A.3d). In Part B, the student indicates that $\frac{2}{1}$ is 2 whole pizzas by agreeing with Peter that the number of pizzas shared can be written as $\frac{2}{1}$ and drawing an illustration of 2 wholes (3.NF.A.3c). The student creates accurate diagrams showing $\frac{5}{6}, \frac{4}{6}$, and $\frac{3}{6}$ in Part A, $\frac{2}{1}$ in Part B, and $\frac{1}{2}$ in Part C (MP4). In Part A, by providing only a diagram without explaining further with words the relevance of the numerator and same denominator, the student does not provide a precise explanation of why one amount is greater than the other amount, with reference to the denominators and the numerators of the fractions being compared (no credit for MP6). In Parts B and C respectively, the student indicates in diagrams that $\frac{2}{1}$ is two wholes and that $\frac{1}{2}$ is less than a whole by showing a whole with only half shaded (MP7).

Total Awarded Points: 4 out of 5

Sharing Pizza Task
Jenny, Kim, and Peter share two pizzas that are the same size. Jenny eats $\frac{5}{6}$ of a whole pizza, Kim eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.
a. Who eats more pizza, Peter or Jenny? Use $<,>$, or $=$ to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use diagrams and words to explain how the numerator and denominator of the fractions can help you figure out which student eats more pizza.


Litho\#: 00063200144

Sharing Pizza Task
Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kim claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter.

c. Explain with words and a diagram why you agree or disagree with Kim.


Litho\#: 00063200144

## Anchor 5

Litho 00063200144
Total Content Points: 2 (3.NF.A.3d, 3.NF.A.3c)
Total Practice Points: 1 (MP6)
In Part A, the student compares two fractions with the same denominator by recording the results of the comparison with the appropriate inequality symbol, writing " $\frac{5}{6}>\frac{4}{6}$ " (3.NF.A.3d). In Part B, the student indicates that $\frac{2}{1}$ is 2 whole pizzas by agreeing with Peter and drawing an illustration of 2 wholes, each divided into sixths, and stating that "they ate 12 pizzas total and you turn the 12 to a two" (3.NF.A.3c). Although the student creates accurate diagrams for $\frac{5}{6}$ and $\frac{4}{6}$ in Part A and $\frac{2}{1}$ in Part B, there is not an accurate diagram showing $\frac{1}{2}$ (no credit for MP4). In Part A, the student indicates a precise explanation of why one amount is greater than the other amount by making reference to the denominators and the numerators of the fractions being compared ("The Numorator and denominator helped me because they had the same denominator so I just looked at the Numorator") (MP6). The student does not indicate in written explanation or diagram that $\frac{1}{2}$ is less than a whole (no credit for MP7).

Total Awarded Points: 3 out of 5

Sharing Pizza Task
Jenny, Kim, and Peter share two pizzas that are the same size. Jenny eats $\frac{5}{6}$ of a whole pizza, Kım eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.
a. Who eats more pizza, Peter or Jenny? Use $<,>$, or $=$ to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use diagrams and words to explain how the numerator and denominator of the fractions can help you figure out which student eats more pizza.


Lltho\#: 00453200107

Sharing Pizza Task
Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kım claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter.

c. Explain with words and a diagram why you agree or disagree with Kım.
 they ohared twopizza.

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Anchor 6
Total Content Points: 2 (3.NF.A.3d, 3.NF.A.3c)
Total Practice Points: 1 (MP7)
In Part A, the student compares two fractions with the same denominator by recording the results of the comparison with the appropriate inequality symbol, writing "Jenny > Peter," which represents the correct relationship between the fractions (3.NF.A.3d). In Part B, the student indicates that $\frac{2}{1}$ is 2 whole pizzas by agreeing with Peter that the number of pizzas shared can be written as $\frac{2}{1}$ and stating that "they share two pizza" (3.NF.A.3c). Although the diagrams in Part A are divided into the correct number of pieces, the pieces are of unequal shape and size, thereby inaccurately modeling $\frac{4}{6}$ and $\frac{5}{6}$ (no credit for MP4). The student does not indicate a precise explanation of why one amount is greater than the other amount, making reference to the denominators and the numerators of the fractions being compared (no credit for MP6). In Part B, the student indicates in a written explanation that $\frac{2}{1}$ is two wholes ("they share two pizza") and shows a diagram of two whole pizzas (unequal size and shape pieces notwithstanding). In Part C, the student indicates that $\frac{1}{2}$ is less than a whole by creating a diagram showing a whole with only half shaded (MP7).

Total Awarded Points: 3 out of 5

A-7a

## Sharing Pizza Task

 Jenny, Kim, and Peter share two pizzas that are the same size, Jenny eats $\frac{5}{6}$ of a whole pizza, Kim eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.a. Who eats more pizza, Peter or Jenny? Use $<,>$, or $=$ to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use diagrams and words to explain how the numerator and denominator of the fractions can help you figure out which student eats more pizza.


Sharing Pizza Task
Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kim claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter

$$
\frac{2}{1}=2
$$

I agree with Peter because in all the three friends ate 12 slices of Pizza. Each Pizza had 6 slices and $6 \times 2=1250$ they final ate Pizzas
c. Explain with words and a diagram why you agree or disagree with Kim. * If they only ate half both of the pizzas than they would have only ate 6 slices and each friend wand have ate 2 slices

Total Content Points: 2 (3.NF.A.3d, 3.NF.A.3c)

## Total Practice Points: 0

In Part A, the student compares two fractions with the same denominator by recording the results of the comparison with the appropriate inequality symbol, writing " $\frac{5}{6}>\frac{4}{6}$ " (3.NF.A.3d). In Part B, the student indicates that $\frac{2}{1}$ is 2 whole pizzas (" $\frac{2}{1}=2$ ") (3.NF.A.3c). The student does not create accurate diagrams showing $\frac{5}{6}, \frac{4}{6}, \frac{2}{1}$, and $\frac{1}{2}$ (no credit for MP4). While the student does refer to the numerators of the fractions being compared, the explanation is insufficient without reference to the significance of the denominators being the same, thereby not providing a precise explanation of why one amount is greater than the other amount (no credit for MP6). The student does not indicate with a written explanation or diagram that $\frac{1}{2}$ is less than a whole (no credit for MP7).

Total Awarded Points: 2 out of 5

## A-8a

## Sharing Pizza Task

Jenny, Kim, and Peter share two pizzas that are the same size. Jenny eats $\frac{5}{6}$ of a whole pızza, Kim eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.
a. Who eats more pizza, Peter or Jenny? Use <, >, or $=$ to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use dragrams and words to explain how the numerator and denominator of the fractions can help you figure out which student eats more pizza.


Sharing Pizza Task
Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kim claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter.

c. Explain with words and a diagram why you agree or disagree with Kim.


Litho\#: 00033200103

## Total Practice Points: 0

In Part A, the student compares two fractions with the same denominator by recording the results of the comparison with the appropriate inequality symbol, writing " $\frac{5}{6}>\frac{4}{6}$ " (3.NF.A.3d). In Part B, the student does not indicate that $\frac{2}{1}$ is 2 whole pizzas (no credit for 3.NF.A.3c). The student does not create accurate diagrams showing $\frac{2}{1}$ and $\frac{1}{2}$ (no credit for MP4). While the student does refer to the numerators of the fractions being compared, the explanation is insufficient without reference to the significance of the denominators being the same, thereby not providing a precise explanation of why one amount is greater than the other amount (no credit for MP6). The student does not indicate in written explanation or diagram that $\frac{1}{2}$ is less than a whole or that $\frac{2}{1}$ is two wholes (no credit for MP7).

## Total Awarded Points: 1 out of 5

## Sharing Pizza Task

Jenny, Kım, and Peter share two pizzas that are the same size. Jenny eats $\frac{5}{6}$ of a whole pizza, Kim eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.
a. Who eats more pizza, Peter or Jenny? Use $<,>$, or $=$ to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use diagrams and words to explain how the numerator and denominator of the fractions can help you figure out which student eats more pizza.


Sharing Pizza Task
Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kim claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter.

c. Explain with words and at diagram why you agree or disagree with Kim.


Litho\#: 00013200107

Total Content Points: 1
(3.NF.A.3d)

## Total Practice Points: 0

In Part A, the student compares two fractions with the same denominator by drawing a visual fraction model with one part representing the amount Jenny ate $\left(\frac{5}{6}\right)$, and the other part representing the amount $\operatorname{Kim}$ ate $\left(\frac{3}{6}\right)$, with a correctly used inequality symbol to represent the relationship between them (3.NF.A.3d). The student does not indicate that $\frac{2}{1}$ is 2 whole pizzas (no credit for 3.NF.A.3c). Though the student creates accurate diagrams showing $\frac{5}{6}$ and $\frac{3}{6}$, there are no clear diagrams representing $\frac{2}{1}$ or $\frac{4}{6}$ (no credit for MP4). The student does not provide any explanation of why one amount is greater than the other amount, making reference to the denominators and the numerators of the fractions being compared (no credit for MP6). The student does not indicate in written explanation or diagram that $\frac{1}{2}$ is less than a whole or that $\frac{2}{1}$ is two wholes (no credit for MP7).

Total Awarded Points: 1 out of 5

A-10a

Sharing Pizza Task
Jenny, Kim, and Peter share two pizzas that are the same size. Jenny eats $\frac{5}{6}$ of a whole pizza, Kim eats $\frac{3}{6}$ of a whole pizza, and Peter eats $\frac{4}{6}$ of a whole pizza.
a. Who eats more pizza, Peter or Jenny? Use $<,>$, or $=$ to compare the fraction of a pizza Jenny eats with the fraction of a pizza Peter eats. Use diagrams and words to explain how the numerator and denominator of the fractions can help you figure out which student eats more pizza.
Jenny ate more pizza than
Peter becouse if you look at the factions it show that Jenny ate more because $\frac{5}{6}$ is more than $\frac{4}{6}$ if you draw a pizza like this $\frac{5}{2}$ that Jenny at more because She only left I slice and peter left 3 slices. $6-5=1$ and $6-3=3$.

A-10b

Sharing Pizza Task
Peter claims that the number of pizzas the three friends share can be written as $\frac{2}{1}$, but Kim claims the number of pizzas can be written as $\frac{1}{2}$.
b. Explain with words and a diagram why you agree or disagree with Peter.

I disagree with peter becouse 2 slices of pizea is going to make more. pieczs but I agree with kim becouse lowhole pizza can be cut into 2 pieces.
c. Explain with words and a diagram why you agree or disagree with Kim.


## Total Content Points: 0

## Total Practice Points: 0

Although the student states in Part A that " $\frac{5}{6}$ is more than $\frac{4}{6}$," the student does not compare two fractions with the same denominator by recording the results of the comparison with the symbols > or < (no credit for 3.NF.A.3d). The student does not state that $\frac{2}{1}$ is 2 whole pizzas (no credit for 3.NF.A.3c). Although the student shows accurate diagrams for $\frac{5}{6}$ and $\frac{3}{6}$, there are no diagrams showing $\frac{2}{1}$ and $\frac{1}{2}$ (no credit for MP4). The student does not indicate a precise explanation of why one amount is greater than the other amount, making reference to the denominators and the numerators of the fractions being compared (no credit for MP6). The student does not indicate in written explanation or diagram that $\frac{1}{2}$ is less than a whole or that $\frac{2}{1}$ is two wholes (no credit for MP7).

Total Awarded Points: 0 out of 5

